7 A Survey of Swarm Algorithms Applied to Discrete Optimization Problems

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7.1 Introduction

Swarm-based algorithms are inspired by the behavior of some social living beings, such as ants, termites, birds, and fishes. Self-organization and decentralized control are remarkable features of swarm-based systems that, such as in nature, lead to an emergent behavior. Emergent behavior is a property that emerges through local interactions among system components and it is not possible to be achieved by any of the components of the system acting alone (Garnier et al., 2007).

In the beginning, the two mainstreams of the Swarm Intelligence area were ant colony optimization (Dorigo and Stützle, 2004) and particle swarm optimization (PSO) (Kennedy and Eberhart, 2001). In recent years, new swarm intelligence algorithms have appeared, inspired by fish schools (Cai, 2010), gravity and mass interactions (Rashedi et al., 2009), as well as different aspects of the behavior of bees (Abbass, 2001b; Karaboga, 2005; Lucic and Teodorovic, 2002; Pham et al., 2005), bacteria (Passino, 2002), glowworms (Krishnanand and Ghose, 2005), fireflies (Yang, 2008), cockroaches (Havens et al., 2008), bats (Yang, 2009), and cuckoo birds (Yang and Deb, 2009). For a thorough review of recent approaches, see Parpinelli and Lopes (2011). Despite the swarm inspiration common to these approaches, they have their own particular way to exploit and explore the search space of the problem.

Although almost all the above cited algorithms were designed to be applied to continuous optimization, several of them were later adapted to handle discrete domain problems. Unlike the continuous domain, in which the elements have the

property of varying smoothly, the elements inside a discrete domain—such as integers or binary digits—accept only distinct, separated values. The discrete domain is characterized by dealing with countable sets, either finite or infinite. Binary and combinatorial applications are examples of discrete domain problems.

This work reviews how swarm algorithms, that traditionally deal with continuous domains, can be adapted to discrete problems. In this work, we highlighted their adaptation strategies to handle this class of problems as well as their main features concerning the problem being solved. Note that algorithms created specifically to handle discrete problems are beyond the scope of this work. This is the case, for instance, of the ant colony optimization algorithm (Dorigo and Stützle, 2004), the mosquito host-seeking algorithm (Feng et al., 2009), the calling behavior of Japanese tree frogs algorithm (Hernández and Blum, 2012), the river formation dynamics algorithm (Rabanal et al., 2007), and the intelligent water drops algorithm (Shah-Hosseini, 2007).

Section 7.2 shortly describes the bioinspirations of the main swarm algorithms adapted to discrete problems; Section 7.3 brings the main concerns to handle discrete problems, the discretization methods, and the encoding strategies; Section 7.4 details all the problems and applications addressed by each continuous algorithm; Section 7.5 summarizes and discusses the main issues; and Section 7.6 presents the concluding remarks and points future research directions.

7.2 Swarm Algorithms

For all traditional versions of the algorithms discussed in this survey, in their essence, the candidate solutions are encoded as a set of real variables, which represent a point in a multidimensional space. In this section, we briefly describe the swarm algorithms that are applied or adapted to handle discrete problems.

7.2.1 Particle Swarm Optimization

The PSO metaheuristics was motivated by the coordinate movement of fish schools and bird flocks (Kennedy and Eberhart, 2001). A potential solution to the problem being solved is represented by a particle, and the PSO is a swarm of particles. Particles "flow" through hyperdimensional search space of the problem, and changes to the position of the particles within the search space are based on the sociocognitive tendency of individuals to emulate the success of other individuals. Each individual of a population (in this case, particles) has its own life experience and is able to evaluate the quality of its experience. As social individuals, they also have knowledge about how well their neighbors have behaved. These two kinds of information correspond to the cognitive component (individual learning) and social component (cultural transmission), respectively. Hence, an individual decision is taken considering both the cognitive and social components, thus leading the population (the swarm) to an emergent behavior.

7.2.2 Roach Infestation Optimization

The roach infestation optimization (RIO) was introduced by Havens et al. (2008), who applied to benchmark functions and achieved competitive results, when compared to a standard PSO. Actually, RIO has some elements that resemble the traditional PSO algorithm. In the RIO algorithm, cockroach agents are defined using three simple behaviors:

- **1.** Cockroaches search for the darkest location in the search space and the fitness value is directly proportional to the level of darkness (find darkness phase).
- 2. Cockroaches socialize with nearby cockroaches (find friend phase).
- **3.** Cockroaches periodically become hungry and leave the friendship to search for food (find food phase).

7.2.3 Cuckoo Search Algorithm

Cuckoo search algorithm (CSA) (Yang and Deb, 2009) is based on the brood parasitism of some cuckoo species. The algorithm uses the Levy flights rather than simple random walk. The CSA uses the following main basic rules:

- 1. Each cuckoo lays one egg at a time and dumps its egg in a randomly chosen nest.
- 2. The best nests with high-quality eggs will continue to the next generation.
- **3.** The number of available host nests is fixed, and the egg laid by a cuckoo is discovered by the host bird with a probability $p_a \in [0,1]$. In this case, the host bird can either get rid of the egg or simply abandon the nest and build a new nest.

7.2.4 Firefly Algorithm

The firefly algorithm (FA) was proposed by Yang (2008) and uses three main basic rules:

- 1. A firefly will be attracted by other fireflies regardless their sex.
- **2.** Attractiveness is proportional to their brightness and decreases as the distance among them increases.
- 3. The landscape of the objective function determines the brightness of a firefly.

7.2.5 Gravitational Search Algorithm

The gravitational search algorithm (GSA) was created based on the law of gravity and the notion of mass interactions (Rashedi et al., 2009). The GSA uses the theory of Newtonian physics and its searcher agents are the collection of masses. In GSA, there is an isolated system of masses; using the gravitational force, every mass in the system can detect the situation of other masses. The gravitational force is therefore a way of transferring information between different masses. The GSA agents are considered as objects and their performance is measured by their masses. All these objects attract each other by a gravity force, and this force causes a movement of all objects globally toward the objects with heavier masses. The heavy masses correspond to good solutions of the problem. The position of the agent corresponds to a solution of the problem, and its mass is determined using a fitness function.

7.2.6 Bat Algorithm

The bat algorithm (BA) was first presented by Yang (2010). The basic idea behind the BA is that a population of bats (possible solutions) use echolocation to sense distance and fly randomly through a search space updating their positions and velocities. The bats' flight aims at finding food/prey (best solutions). A loudness decay factor acts in a similar role as the cooling schedule in the traditional simulated annealing optimization method, and a pulse increase factor regulates the pulse frequency. As the loudness usually decreases once a bat has found its prey/solution (in order to not to loss the prey), the rate of pulse emission increases in order to raise the attack accuracy.

7.2.7 Glowworm Swarm Optimization Algorithm

The glowworm swarm optimization (GSO) algorithm was first presented by Krishnanand and Ghose (2005) as an application to collective robotics. In this algorithm, each glowworm uses a probabilistic mechanism to select a neighbor that has a luciferin value associated with him and moves toward it. Glowworms are attracted to neighbors that glow brighter (i.e., glowworms that have more luciferin). The movements are based only on local information and selective neighbor interactions. This enables the swarm to divide into disjoint subgroups that can converge to multiple optima of a given multimodal function.

7.2.8 Artificial Fish School Algorithm

In water areas, a fish can always find food at a place where there are plenty of food by following other fishes, hence generally the more the food, the more the fish. Following this rule, artificial fish school algorithm (AFSA) builds some artificial fish (AF), which search an optimal solution in solution space (the environment in which AF live) by imitating fish swarm behavior. Three basic behaviors of AF are defined as follows (Cai, 2010):

- **1.** *Prey*: The fish perceives the concentration of food in water to determine the movement by vision or sense and then chooses the tendency.
- **2.** *Swarm*: The fish will assemble in groups naturally during the moving process, which is a kind of living habits in order to guarantee the existence of the colony and avoid dangers.
- **3.** *Follow*: In the moving process of the fish swarm, when a single fish or several fishes find food, the neighborhood partners will trail and reach the food quickly.

7.2.9 Bacterial Evolutionary Algorithm

The bacterial evolutionary algorithm (BEA) is inspired by bacteria's behavior. Bacteria can transfer DNA to recipient cells through mating and this process is called transduction. By transduction, it is possible to spread the features of a single bacterium to the rest of the population. This genetic recombination mechanism characterizes a microbial evolution process. Male cells directly transfer strands of genes to female cells. After that, those female cells acquire characteristics of male cells and transform themselves into male cells, thus spreading to the entire bacteria population. Genes can be transferred from a single bacterium (host cell) to others (recipient cells) and eventually this would lead to an increase in the evolution speed of the entire population (Nawa and Furuhashi, 1999). The flow of the BEA is described as follows:

- 1. Generation of the initial population: Chromosomes are randomly created and evaluated.
- 2. Bacterial mutation: The bacterial mutation is applied to each chromosome, one by one.
- 3. Gene transfer operation: The gene transfer operation occurs between the chromosomes.

7.2.10 Bee Algorithm

The bee algorithm¹ (BA₁) was first introduced by Pham et al. (2005) and applied to a benchmark of mathematical functions. In this algorithm, a bee is a *d*-dimensional vector containing the problem variables (a solution). Moreover, a solution represents a visited site (i.e., food source) and has a fitness value assigned to it. The algorithm balances exploration and exploitation by using scout bees that randomly search for new sites and uses recruitment for neighborhood search in sites with higher fitness, respectively. Bees that have the highest fitness are chosen as "selected bees" and sites visited by them (elite sites) are chosen for neighborhood search. The algorithm conducts searches in the neighborhood of the selected sites, assigning more bees to search near to the best sites (recruitment).

7.2.11 Artificial Bee Colony Algorithm

The artificial bee colony (ABC) algorithm was first proposed by Karaboga (2005) for solving multidimensional and multimodal optimization problems. The bees' aim is to discover places of food sources (regions in the search space) with high amount of nectar (good fitness). There are three types of bees: the scout bees that randomly fly in the search space without guidance, the employed bees that exploit the neighborhood of their locations selecting a random solution to be perturbed, and the onlooker bees that use the population fitness to select probabilistically a guiding solution to exploit its neighborhood. If the nectar amount of a new source is higher than the previous one in their memory, they update the new position and forget the previous one (greedy selection). If a solution is not improved by a

¹The subindex 1 is introduced here to differentiate the bee algorithm from the bat algorithm.

predetermined number of trials, then the food source is abandoned by the corresponding employed bee and it becomes a scout bee.

7.2.12 Bee Colony Optimization

The bee colony optimization (BCO) was proposed by Lucic and Teodorovic (2002) and, similarly to ABC, it imitates the bees' behavior in nature when looking for a food, by simulating the foraging behavior. The BCO is based on the constructive concept. It was designed as a method which builds solutions from the scratch within execution steps, unlike the ABC local search which performs iterative improvements of the current best solution. There are two alternating phases of the BCO (forward pass and backward pass) constituting a single step in the BCO algorithm. In each forward pass, every bee agent visits the solution components, creates a partial solution, and after that returns to the hive. Having obtained new partial solutions, the bees meet in the hive and start the backward pass. In the backward pass, all bee agents share information about the quality of their partial solutions. Having all solutions evaluated, each bee decides with a certain probability whether it will stay loyal to its solution or not.

7.2.13 Marriage in Honey-Bees Optimization Algorithm

The marriage in honey-bees optimization (MBO) algorithm was presented by Abbass (2001b). The main idea concerning the algorithm based on bee mating behavior is that the queen is considered the best solution to an optimization problem and, during the mating flight, it selects drones probabilistically for reproduction so as to form the spermatheca. The spermatheca is, then, a pool of selected solutions. New broods are created by crossovering the genotypes of drones and the queen. Natural selection takes place by replacing weaker queens by fitter broods.

7.3 Main Concerns to Handle Discrete Problems

In most swarm intelligence algorithms, the possible solution is encoded as a set of real variables, which represents, for instance, the location of a particle (in PSO) or a source food (in ABC). In these examples, updates in a given vector position (dimension) can be done independently of the remaining ones. The updated values remain within the predefined range for that dimension, the candidate solution is valid (for the sake of simplification, constraints are not considered here). However, for combinatorial problems, such representation is not suitable, provided that a solution is a permutation of integer values. Therefore, updates of a vector that represents a solution for a combinatorial problem must preserve the validity of the permutation. Consequently, to apply the above-mentioned algorithms to discrete optimization problems, it is necessary to adapt the encoding to discrete dimensions.

We characterize the codification of candidate solutions in three encoding schemes. The first encoding uses a binary codification (BC) for candidate solutions. The second encoding uses an integer codification (IC) for candidate solutions. Swarm algorithms that employ BC or IC are adapted to discrete domain since its beginning (i.e., initial swarm). The third encoding deals with real values but uses transformation methods to handle discrete domains. The real solution vector can be transformed into a BC (real-to-binary: RTB) or it can be transformed into an IC (real-to-integer: RTI), where RTI represents a combination of integer values. Swarm algorithms that employ RTB or RTI require these transformations at each iteration loop.

7.3.1 Discretization Methods

In discrete problems, such as combinatorial, binary, and categorical, it is necessary to reduce the number of possible states to feasible solutions. This is done by the discretization of the continuous space by transforming the values into a limited number of possible states. There are several discretization methods, and the main are presented below.

7.3.1.1 Sigmoid Function

The sigmoid function (SF) can be used to transform a continuous space value into a binary one. Such discretization method is very popular (Banati and Bajaj, 2011; Palit et al., 2011), and the transformation is applied to each dimension of the solution vector, as shown in Eq. (7.1), thus forcing each element to be a binary digit:

$$x_{ij} = \begin{cases} 1, & \text{if rand}() \le \frac{1}{1 + \exp(-x_{ij})} \\ 0, & \text{otherwise} \end{cases}$$
(7.1)

with i = 1, ..., N, j = 1, ..., D, where N is the population size, D is the dimension size, and rand() is a random number drawn uniformly from [0,1].

7.3.1.2 Random-Key

The random-key (RK) encoding scheme can be used to transform a position from a continuous space into an integer/combinatorial space (Chen et al., 2011; Li et al., 2010). To decode the position, the nodes are visited in ascending order for each dimension. For example, the continuous solution vector $\vec{x_i} = (0.90, 0.35, 0.03, 0.21, 0.17)$ can be decoded as $\vec{x_i} = (5, 4, 1, 3, 2)$.

7.3.1.3 Smallest Position Value

The smallest position value (SPV) method maps the positions of the solution vector by placing the index of the lowest valued component as the first item on a permutated solution, the next lowest as the second, and so on. This method creates an integer vector solution by indexing the position of all the particles (Verma and Kumar, 2012; Yousif et al., 2011).

7.3.1.4 Modified Position Equation

The modified position equation (MPE) method has been used only in the PSO algorithm (Pan et al., 2008; Tasgetiren et al., 2007). As mentioned before, the standard PSO updates the particle position using three choices: follow its own position (X_i^t) , go toward its personal best position (P_i^t) , or go toward the best particle position of the swarm (G_i^t) . After that, the particle position on iteration *t* can be updated following Eq. (7.2):

$$X_{i}^{t} = c_{2} \otimes F_{3}(c_{1} \otimes F_{2}(\omega \otimes F_{1}(X_{i}^{t-1}), P_{i}^{t-1}), G_{i}^{t-1})$$
(7.2)

where $\lambda_i^t = w \otimes F_1(X_i^{t-1})$ is the velocity of the particle and F_1 is the mutation operator with probability w. A uniform random number r in the range [0,1] is generated and, if it is less than w, then the mutation operator is applied to generate a perturbed permutation of the particle by $\lambda_i^t = F_1(X_i^{t-1})$; otherwise current permutation is kept as $\lambda_i^t = X_i^{t-1}$. In this equation, $\delta_i^t = c_1 \otimes F_2(\lambda_i^t, P_i^{t-1})$ is the cognitive part of the particle; F_2 is the crossover operator with probability c_1 . Note that λ_i^t and P_i^{t-1} will be the first and second parents for the crossover operator. It results either in $\delta_i^t = F_2(\lambda_i^t, P_i^{t-1})$ or in $\delta_i^t = \lambda_i^t$ depending on the choice of a uniform random number. The third component of Eq. (7.2), $X_i^t = c_2 \otimes F_3(\delta_i^t, G_i^t)$, is the social part of the particle, where F_3 is the crossover operator with probability c_2 . Note that δ_i^t and G_i^{t-1} will be the first and second parents for the crossover operator. It results either in $X_i^t = F_3(\delta_i^t, G_i^{t-1})$ or in $X_i^t = \delta_i^t$ depending on the choice of a uniform random number. The third component of Eq. (7.2), $X_i^t = c_2 \otimes F_3(\delta_i^t, G_i^t)$, is the social part of the particle, where F_3 is the crossover operator with probability c_2 . Note that δ_i^t and G_i^{t-1} will be the first and second parents for the crossover operator. It results either in $X_i^t = F_3(\delta_i^t, G_i^{t-1})$ or in $X_i^t = \delta_i^t$ depending on the choice of a uniform random number.

7.3.1.5 Great Value Priority

The great value priority (GVP) method is used to encode a continuous space into a binary one (Congying et al., 2011). First, the position of the solution vector $\vec{x_i}$ with the largest element is selected, where i = 1, ..., N and N is the population size. This position is set on the first position of a new vector named as permutation vector \vec{p} . Next, the position of the second largest element of $\vec{x_i}$ is selected and placed in the next position of \vec{p} . This procedure is repeated successively for all dimensions of $\vec{x_i}$ and, once \vec{p} is fulfilled, Eq. (7.3) is applied to transform it into binary, where j = 1, ..., D and D is the dimension size:

$$\vec{x}_{ij} = \begin{cases} 1, & \text{if } \vec{p}_j > \vec{p}_{j+1} \\ 0, & \text{otherwise} \end{cases}$$
(7.3)

7.3.1.6 Nearest Integer

In this method, a real value is converted to the nearest integer (NI) by rounding or truncating up or down (Burnwal and Deb, 2012).

7.4 Applications to Discrete Problems

For the algorithms mentioned in Section 7.2, a literature search was done so as to find discrete applications in different domains. Although this search was not exhaustive, it covers the most relevant applications and emphasizes the applicability of those algorithms to discrete problems.

7.4.1 Particle Swarm Optimization

Kennedy and Eberhart (1997) developed the first PSO algorithm for combinatorial optimization problems, where particles were encoded as binary sequences. In the binary version, trajectories are changes in the probability that a coordinate will take a zero or one value. Also, the velocity of the particle may be described by the number of bits changed per iteration or the Hamming distance between the particle at time *t* and t + l.

Deep and Bansal (2008), Hembecker et al. (2007), Shen et al. (2012), and Wan and Nolle (2009) used the SF method to calculate the trajectory in the binary search space to solve the Knapsack problem (KP). For the same problem, Lopes and Coelho (2005) used a PSO hybridized with a guided local search and some concepts drawn from genetic algorithms (GA). In Li and Li (2009), a binary PSO is proposed to solve the KP using a mutation operator.

A PSO was used to solve the flow shop scheduling problem by Ucar and Tasgetiren (2006). First, a population of particles with continuous values is randomly constructed and then transformed into discrete values by applying the SPV method. The same method was used to solve the single machine total-weighted tardiness problem by Tasgetiren et al. (2004a,b), where the SPV rule is applied to convert the position vector to a job permutation. Verma and Kumar (2012) also used PSO with SPV to solve a combinatorial optimization problem, the DNA sequence assembly. Lin et al. (2010) used a continuous PSO combined with the RK transformation to solve the job shop scheduling problem (JSSP). PSO was hybridized with a local search based on simulated annealing (SA) technique.

Congying et al. (2011) used the PSO in a typical combinatorial optimization problem, the quadratic assignment problem (QAP), and the GVP method was used to transform the continuous space to discrete.

Rosendo and Pozo (2010) presented a hybrid PSO algorithm to solve the traveling salesman problem (TSP). This work maintains the main PSO concept for updating the velocity of the particle using path relinking (Glover and Laguna, 1997) and the Lin–Kernighan (LK) algorithm (Lin and Kernighan, 1973) to improve local search.

Labed et al. (2011) proposed MHPSO, a hybrid PSO to solve the multidimensional KP. As in Lopes and Coelho (2005), it combines PSO with the crossover operator of GA. The crossover operator is applied in both the best position of each particle (*pbest*) and its current position, as well as in the best position obtained by the swarm (*gbest*) and its current position.

To the best of our knowledge, Pan et al. (2008) reported for the first time in the literature a discrete particle swarm optimization (DPSO) algorithm to solve the nowait flow shop scheduling problem. The particles are represented as discrete job permutations and a new position update method is developed based on the discrete domain that consists of three operators. A new crossover operator was also introduced, and it is able to produce a pair of different permutations even from two identical parents. A block of jobs from the first parent is determined by two-cut points randomly, and this block is moved to the right or left of the solution vector. Then, the offspring permutation is filled out with the remaining jobs from the second parent. The DPSO algorithm is also hybridized with the variable neighborhood (VND) local search by Mladenovic and Hansen (1997) to improve the performance. Tasgetiren et al. (2007) also used DPSO with the MPE method to solve the generalized TSP.

7.4.2 Roach Infestation Optimization

Hendrawan and Murase (2011) proposed a discrete RIO to solve a feature selection problem using a neural network as a predictive tool. A binary encoding vector was used for each roach, and each dimension represents a feature (value 0 or 1). A 0 indicates that the corresponding feature is not selected, while 1 means the opposite. To update the position of the roach, the cockroach velocity is updated with a mutation operator and then the cognition and social parts of the cockroach are updated using a two-point crossover.

7.4.3 Cuckoo Search Algorithm

Burnwal and Deb (2012) demonstrated for the first time a CSA to solve a scheduling problem for a flexible manufacturing system (FMS). They modified the Levy flights from continuous to discrete values using the NI. For the same type of problem, Kumar and Chakarverty (2011) encoded a solution in the CSA in the form of an integer vector.

Gherboudj et al. (2012) proposed a discrete binary CSA to solve the KP. To get binary solutions, the SF was used and Layeb (2011) presented a quantum-inspired cuckoo search algorithm (QICSA) for the same KP but, instead, a binary encoding was used.

7.4.4 Firefly Algorithm

The first FA for combinatorial optimization was put forward by Sayadi et al. (2010) for makespan minimization in a permutation flow shop scheduling problem.

Also, Falcon et al. (2011) used the same ideas for a fault diagnosis problem. In both cases, they used a binary approach: for updating the firefly's position, and SF was applied to each component of the real-valued vector. The SF method was used to transform the values from real to binary by Palit et al. (2011), for the KP, and by Banati and Bajaj (2011), to solve the binary problem of feature selection.

Yousif et al. (2011) introduced a method based on FA for scheduling jobs on grid computing. In this case, the SPV approach was used for updating the positions of the fireflies from continuous position values to discrete permutations.

Fister et al. (2012) used the FA to solve a combinatorial optimization problem, the graph 3-coloring. The RK method was used to convert the real values to discrete.

7.4.5 Bee Algorithm

The BA1 was first applied to continuous optimization functions and later for scheduling jobs (Pham et al., 2007a) and binary data clustering (Pham et al., 2007b). In these papers, the authors used discrete encoding, ensuring that possible solutions would be valid. The BA1 also inspired Bahamish et al. (2008) to create a discrete encoding for the protein tertiary structure prediction (PTSP), a difficult combinatorial optimization problem.

A well-known discrete problem is the generalized assignment problem (GAP), approached by Ozbakir et al. (2010) using a modified BA. In the original BA_1 , scout bees continue searching in the solution space until the algorithm is terminated. However, in the modified BA_1 , an adaptive penalty coefficient mechanism is employed.

A binary BA_1 (BBA) was proposed by Xu et al. (2010) focusing on a two-level distribution optimization problem (DOP), which expressed the agents (bees) as two binary matrices, representing how to assign each bee to its course or mission.

7.4.6 Artificial Bee Colony

The applicability of the ABC algorithm and the GAP (Baykasoğlu et al., 2007) demonstrates the capability to adapt this algorithm to discrete problems, using the RK method. The ABC was also applied to other discrete problems, such as the JSSP, TSP, and multidimensional KP. For these applications, many variants and hybridisms of the ABC were proposed.

An adaptation of the original ABC method was presented by Banharnsakun et al. (2012) for the JSSP, by changing the behavior of the onlooker bees and using the SF method to transform the continuous values into binary. The proposed new method, called best-so-far ABC, uses all the onlooker bees with the information from all employed bees to make a common decision on a new candidate food source. Because of that, the onlookers can compare information from all candidate sources and they are able to select the best-so-far position. As a result, this modification makes the algorithm converge more quickly since that solution will be biased toward the best solution found so far. A combinatorial ABC (CABC) with discrete encoding was proposed by Karaboga and Gorkemli (2011) for the TSP. In that work, a new mutation operator from GA was used, and it was adapted to the neighborhood search mechanism of employed and onlooker bees. The hybridism between GA and ABC was also approached by Singh et al. (2011), which used ABC techniques to improve the global search by adding employed and onlooker bees on the search process, and this method was called real genetic bee colony algorithm (RGBCA). A similar hybridism, between ABC and greedy subtour crossover (GSX), was used by Banharnsakun et al. (2010) for the same problem. In this hybrid method, the exploitation process of the ABC algorithm was improved by the GSX, so as to update employed bees' old food sources based on their neighboring food sources, assisting the ABC to generate feasible solutions all the time.

The KP is another classical discrete problem that has been studied using the ABC algorithm. Pulikanti and Singh (2009) used a modified and binary version of ABC for this problem. In the original ABC algorithm, the neighborhood of the best found food sources is searched in order to achieve even better food sources. In the novel ABC algorithm, a hybrid probabilistic mutation scheme was performed for searching the neighborhood of food sources. Here the SF method was used again to convert real values into binary.

Hybrid methods have been used to improve the original ABC algorithm, generally associated to a neighborhood search mechanism to improve global searches. Pacurib et al. (2009) uses this improved search, adding a search iteration operator based on the fixed point theorem of contractive mapping in Banach spaces (discrete vector space) with ABC algorithm to solve Sudoku puzzles.

Another hybrid discrete artificial bee colony (DABC) was proposed by Marinakis et al. (2009), using a two-phase algorithm that combines the DABC and the greedy randomized adaptive search procedure (GRASP). This DABC–GRASP algorithm was created for the solution of clustering problems and the two phases consist of the computation of the activated features by the DABC and the computation of the fitness of each food source by the clustering algorithm.

7.4.7 Bee Colony Optimization

The BCO proposed by Teodorovic and Dell'Orco (2005) was applied to the ridematching problem and wavelength assignment (RWA) using a discrete encoding. Later, Banerjee et al. (2008) created a hybrid BCO for modeling process and supply chain scheduling; in this case, the SF method was used to transform the continuous space into binary. Davidovic et al. (2012) also used the BCO algorithm for scheduling independent tasks on homogeneous processors; their approach brings a modified BCO which allows the bees a freedom to generate various solutions leading to a diversification of the search process. Wong et al. (2008a) also studied the BCO and applied it to the TSP.

Chong et al. (2006) described a BCO algorithm based on foraging and waggle dance, using the dance duration as determining factor for selecting a new path. This approach was applied to the JSSP with discrete encoding and a neighborhood

structure to search for feasible solutions and improve prior solutions (Wong et al., 2008b). A set of priority dispatching rules were used to create the initial solutions.

7.4.8 Marriage in Honey-Bees Optimization Algorithm

The MBO algorithm was applied to the propositional satisfiability problems, known as SAT problems (Abbass, 2001b). MBO was applied to 50 variables of the SAT problems with 215 different constraints, presenting good results for this combinatorial optimization problem with a binary encoding. Later, the algorithm was improved in Abbass (2001a) by using a single queen with multiple workers in the colony and also applied to the 3-SAT problem where each constraint contains exactly three variables.

A conventional annealing approach was used by Teo and Abbass (2001) on the mating flight process to balance search exploration and exploitation, and this modified MBO was applied to SAT problems. This algorithm was also applied in datamining (Benatchba et al., 2005) and scheduling problems (Koudil et al., 2007) with the SF method to convert the continuous space into binary.

The SF method was also used by Marinakis et al. (2008) in an MBO hybridized with GRASP for clustering problems with N objects into K clusters. Yang et al. (2007) combined the MBO with the Nelder–Mead method with the objective of improving its performance and thus creating the Nelder-Mead Marriage in Honey Bees (NMMBO) algorithm to be applied to the TSP.

7.4.9 Other Swarm Intelligence Algorithms

The GSA was applied by Li et al. (2010) with the RK discretization method transforming the continuous solutions into discrete ones. Chen et al. (2011) also applied the GSA to solve the TSP with RK, but integrating the SA technique into the algorithm for accomplishing local search. A binary implementation of GSA was proposed by Papa et al. (2011), together with the SF method, and used for a feature selection problem.

Nakamura et al. (2012) proposed a binary version of the BA to solve the hypercube problem, where each bat is a set of binary coordinates. The equation to update the position of the original BA is replaced by the SF method of discretization.

The GSO was applied by Deng-Xu et al. (2011) to solve the multiconstrained Quality of Service (QoS) multicast routing problem using a discrete vector; this problem is a direct application of the well-known TSP.

Xiangyang et al. (2011) proposed the AFSA to solve KP using the RK method. He et al. (2009) proposed the AFSA mapped into the integer space directly, using a method that ensures that the candidate solution stays in integer space throughout the optimization process.

Balazs et al. (2012) proposed a BEA to solve a permutation flow shop problem with a real-valued vector (arrays). The adaptation of real-valued vectors to permutations is done by using the RK method. Inoue et al. (2000) and Miwa et al. (2002) proposed a binary encoding for the BEA to solve the nurse scheduling problem

using mutation and crossover similar to those of GA. Feng and Xiao (2011) applied the same method for a route planning problem.

7.5 Discussion

The algorithms presented in Section 7.2 were originally devised for dealing with continuous search spaces. However, for discrete search spaces, which is the case of binary and combinatorial problems, the key issue is how to adapt the aforementioned algorithms.

In this survey, we selected 64 papers for analysis. Figure 7.1 shows the distribution of the swarm algorithms covered here. It is clearly observed that PSO was the most frequently found algorithm, representing a quarter of all papers analyzed. The ABC algorithm was the second one, representing 13% of the total.

Figure 7.2 summarizes the distribution of the discretization methods (Section 7.3) employed by the algorithms. The most commonly used method is the SF; 62% of the papers used it to transform continuous values into discrete ones. It is worth to mention that SF is also extensively applied in several other areas, such as artificial neural networks, biomathematics, chemistry, and statistics.

The RK method was the second most frequent, found in 18% of the papers. Since this method is exclusive to transform into integer, not binary, when binary values were necessary a combination of the RK method with the GVP was used by Congying et al. (2011). In this combined process, the first stage consisted of transforming the continuous values into discrete using the RK and a second stage using GVP to convert the discrete values in binary ones. The SPV was also used in 10% of the papers to transform continuous into discrete. The MPE method was used in



Figure 7.1 Algorithms distribution.



Figure 7.2 Discretization methods.



Figure 7.3 Discretization methods used in the algorithms.

5% of the papers. This method was combined with a discrete encoding to handle scheduling and TSP problems. The MPE method was used only in PSO algorithms, but it could be adapted to any other algorithm that uses the same main procedures of PSO, i.e., the update of speed and position. Finally, only 3% of the papers used the NI for this same sort of transformation.

Figure 7.3 summarizes how many times each discretization method was used by each algorithm in the papers surveyed. Note that two of them, RIO and GSO, did not use any discretization method. This is due to the straight encoding schemes



(integer or binary) that do not require further discretization. In two papers, there was no enough information for identifying the discretization method used, so they were not counted in Figure 7.3.

Figure 7.4 lists the encoding schemes (BC, IC, RTB, or RTI—see Section 7.3); 19% of the papers preferred to use the encodings directly as binary and 25% as integer. In this approach, the solution vector is discrete and the algorithm code needs to be modified accordingly to work with these values. For this purpose, several authors created a discrete version of the continuous algorithm, e.g., the DPSO, the CABC, and the DABC optimization. The other 55% of papers preferred to use the original continuous encoding then transforming them the real-valued vector into integer or binary, by using one of the methods presented in Section 7.3.

Figure 7.5 is a more detailed view of the previous plot. It summarizes which encoding scheme was used in each algorithm and how many times these schemes were used.

Finally, regarding the application, Figure 7.6 shows the main classes of problems to which the swarm optimization algorithms were applied. Scheduling problems are the most frequently found, closely followed by the KP.

7.6 Concluding Remarks and Future Research

Real-world discrete and combinatorial problems are usually challenging and require computationally intensive algorithms. Swarm intelligence algorithms have been an interesting alternative for providing satisfactory solutions. The individual characteristics of the continuous swarm algorithms are very useful for these applications. However, to apply them to a discrete problem requires adaptation, hybridization, or modification the original algorithms to handle those sort of problems.

The methods used to achieve this purpose are the most diverse. This survey aims to classify the most common discretization methods and encoding strategies



Figure 7.5 Encoding schemes related of swarm algorithms.



Figure 7.6 Applications of the swarm algorithms.

to guide future authors to select the best method and strategy when working with continuous swarm algorithms for discrete problems. The SF and RK discretization methods appeared most times in the literature review. Both methods seek the transformation of the continuous values handled by the algorithms into discrete ones, requiring an adaptation to deal with possible solutions in a discrete environment.

The results achieved by each paper presented in this survey demonstrate how continuous algorithms can be useful in discrete problems. The large number of papers adapting the PSO for classical combinatorial problems such as Knapsack, Scheduling and TSP support this trend. For the scheduling problem, the FA and

BEA also appeared several times, creating a trail for future authors that intend to work with this combinatorial problem.

Although most of swarm algorithms presented in literature are used for continuous domains, they can also provide good solutions for discrete problems. This seems to be an interesting research opportunity, either developing new methodological approaches or applying to specific discrete/combinatorial problems.

Future work points to a more extensive research on different discretization methods and encoding schemes, focusing on expanding the range of possibilities on using continuous algorithms to discrete problems. Therefore, authors will have in the future more alternatives to combine the desired continuous algorithm with combinatorial and binary problems.

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